

THE EFFECT OF STRESS ON FLOW AND TRANSPORT IN FRACTURED ROCK MASSES USING TOUGH-FLAC AND A MODIFIED CRACK TENSOR THEORY

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ABSTRACT

We used a slightly modified version of Oda's crack tensor theory for developing and applying a modeling approach (that we characterize as a discrete continuum) to upscale the hydraulic and mechanical properties of fractured rock masses. The modified crack tensor theory was used to calculate the stress-dependent permeability tensor and compliance tensor for the individual gridblock. By doing this, we transformed a discrete fracture network model into a grid-based continuum model. The methodology was applied to a benchmark test related to fluid flow and transport through a 20 × 20 m model domain of heavily fractured media. This benchmark test is part of the international DECOVALEX project, thus providing us with the opportunity to compare our results with the results of independent models. We conducted the hydro-mechanical analysis with TOUGH-FLAC, a simulator based on the TOUGH2 multiphase flow code and FLAC3D geomechanical code, using a multiple interacting continua (MINC) method to simulate the flow and transport of fractured rock. The results of our simulations were consistent with the results of the other independent modeling approaches.

INTRODUCTION

Coupled hydromechanical effects, such as the effect of stress on permeability, could have a significant impact on flow and transport in fractured rock (Rutqvist and Stephansson 2003). These are complex processes that can be studied using numerical modeling, although not without encountering difficulties related to upscaling and deriving representative values for both mechanical and hydrological parameters. In this

study, our modeling approach is to use a modified version of the crack tensor theory (Oda 1986) to upscale the hydraulic and mechanical properties determined from a discrete-fracture-network model—and then calculate the stress-dependent permeability (Leung et al. 2009). Using this modeling approach, the discrete fracture network was transformed into a grid-based continuum model. We implemented this modeling approach into the framework of TOUGH-FLAC (Rutqvist et al. 2002), a simulator that links the TOUGH2 (Pruess 1999) multiphase fluid flow code with the FLAC3D (Itasca 2006) geomechanical code.

We applied this methodology to a 2D Bench Mark Test (BMT) problem denoted as Task C in the international DECOVALEX project. The BMT consists of a 20×20 m model domain with a 2D fracture-network model (Figure 1) composed of 7797 individual fractures with correlated aperture length. The effects of stress and hydraulic pressure gradients are considered through various boundary conditions (Figure 2).

For the mechanical boundary conditions, we specify a constant vertical stress of 5 MPa at the top and bottom surfaces, whereas a varying horizontal stress is specified for the right- and left-hand side boundaries to capture different fracture shear behaviors inside the model (Figure 2). We apply the horizontal stress with increasing magnitude, corresponding to the stress ratio (K) of horizontal/vertical stress, varying from 1,2,3,5, to progressively induce shear failure along fractures within the model.

At each set of the stress boundary conditions (after the model is in an equilibrium state), fluid flow and transport through the model is simulated by the specific hydraulic boundary conditions representing a hydraulic gradient P1-P2 (Figure 2). For such hydraulic boundary conditions, a constant pressure gradient of 1.0×10^4 Pa/m and 10 Pa/m is simulated.

The mechanical properties of the rock matrix and fractures are listed in Table 1. For simplicity, mechanical and hydraulic apertures are assumed to be equal.

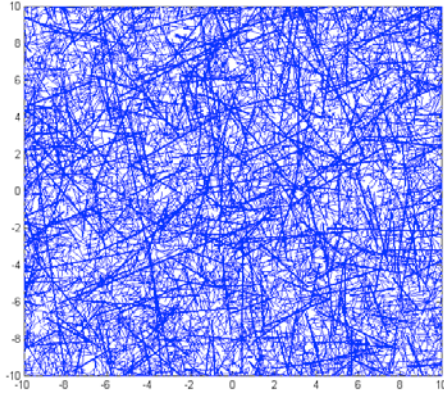


Figure 1. 2D BMT fracture network

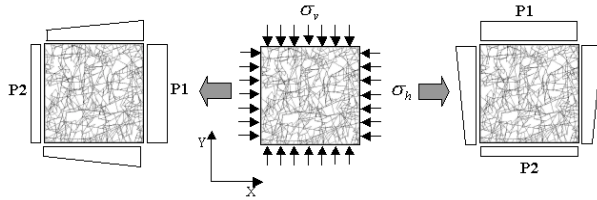


Figure 2. Mechanical and hydraulic boundary conditions

METHODOLOGY

Modified Crack Tensor Theory

According to the BMT definition, the normal stiffness of a single fracture is linked to the normal stress and initial fracture aperture by (Baghbanan and Jing 2008)

$$K_n = \frac{(10\sigma_n + \sigma_{nc})^2}{9\sigma_{nc}b_0} \quad (1)$$

where σ_n is normal stress across the fracture, b_0 is the initial aperture, and σ_{nc} is critical normal stress defined as $\sigma_{nc}[\text{MPa}] = 0.487 \times b_0[\mu\text{m}] + 2.51$. A constant shear stiffness of $K_s = 434$ (GPa) is used for simplicity (Table 1).

Table 1. Model properties of intact rock and fractures

Properties		Value
Intact rock	Elastic modulus, E (GPa)	84.6
	Poisson's ratio, ν	0.24
Fractures	Shear stiffness, K_s (GPa/m)	434
	Friction angle, ϕ ($^\circ$)	24.9
	Dilation angle, d ($^\circ$)	5
	Cohesion, c (MPa)	0
	Critical shear displacement for dilation, U_{cs} (mm)	3
	Minimum aperture value, a_{res} (μm)	1
	Maximum aperture value, a_{max} (μm)	200

The anisotropy for the permeability and elastic stiffness was obtained using Oda's crack tensor theory, using the theory to formulate a discrete summation of contributions from each fracture that intersect an element volume. We could apply this discrete summation approach because the description of fractures given by the Task C BMT definition is explicit: each fracture is known by its position, its geometric properties-length orientation, and aperture. The basic quantities of the crack tensor for each crack in an element are as follows:

$$F_{ij} = \frac{1}{V_e} \frac{\pi}{4} D^3 n_i n_j \quad (2)$$

$$F_{ijkl} = \frac{1}{V_e} \frac{\pi}{4} D^3 n_i n_j n_k n_l \quad (3)$$

$$P_{ij} = \frac{1}{V_e} \frac{\pi}{4} D^2 b^3 n_i n_j \quad (4)$$

where F_{ij} , F_{ijkl} , P_{ij} are basic crack tensors, V_e is the element volume, D is the diameter of the crack, b is the aperture of the crack, and \mathbf{n} is the unit vector of normal orientation for each crack with the component n_i ($i=1,2,3$).

By using the basic crack-tensor quantities defined in Equations (2), (3) and (4) and the mechanical properties for each fracture, we calculate the anisotropic compliance tensor C_{ijkl} and permeability tensor k_{ij} using

$$C_{ijkl} = \sum^{NCR} \left[\left(\frac{1}{K_n D} - \frac{1}{K_s D} \right) F_{ijkl} + \frac{1}{4K_s D} (\delta_{ik} F_{jl} + \delta_{jk} F_{il} + \delta_{il} F_{jk} + \delta_{jl} F_{ik}) \right] \quad (5)$$

$$k_{ij} = \sum^{NCR} \frac{1}{12} (P_{kk} \delta_{ij} - P_{ij}) \quad (6)$$

where NCR is number of cracks in an element and δ_{ij} is Kronecker's delta. So the total elastic compliance tensor can be formulated as

$$T_{ijkl} = C_{ijkl} + M_{ijkl} \quad (7)$$

$$M_{ijkl} = (1/E)[(1+\nu)\delta_{ik}\delta_{jl} - \nu\delta_{ij}\delta_{kl}] \quad (8)$$

where M_{ijkl} is the elastic compliance tensor of the intact rock.

Stress/Aperture Coupling Considering Shear Dilation

The stress effect on the permeability tensor was evaluated for each element, considering stress-induced aperture changes for each fracture intersection of the element. Stress-induced aperture change is expressed as follows:

$$b = b_0 - \delta + \Delta b_{dil} \quad (9)$$

$$\delta = \frac{9\sigma_n b_0}{\sigma_{nc} + 10\sigma_n} \quad (10)$$

where δ is normal closure caused by an increase in normal stress, and Δb_{dil} is dilatational normal displacement. Eq. (10) displays the typical nonlinear normal stress/aperture relationship for rock fractures (Baghbanan and Jing 2008).

The approach for modeling shear dilation is shown in Figure 3. If the shear stress τ on a fracture is below the critical shear stress τ_{sc} (Region 1), no normal displacement resulting from shear occurs. When the shear stress is larger than the critical shear stress (Region 2), slip occurs, and the fracture shear stiffness in Region 2 is calculated using Eq.(11):

$$K_{s2} = \eta \frac{G}{r} \quad (11)$$

where G is the shear modulus of the intact rock, r is the radius of the fracture, and η is a factor with a value that depends upon the geometry of the slip patch. In our case, we may consider a circular crack in which $\eta = 7\pi/24$. Thus, the

dilatational normal displacement can be calculated using

$$\Delta b_{dil} = \frac{\tau - \tau_{sc}}{K_{s2}} \times \tan(d) \quad (12)$$

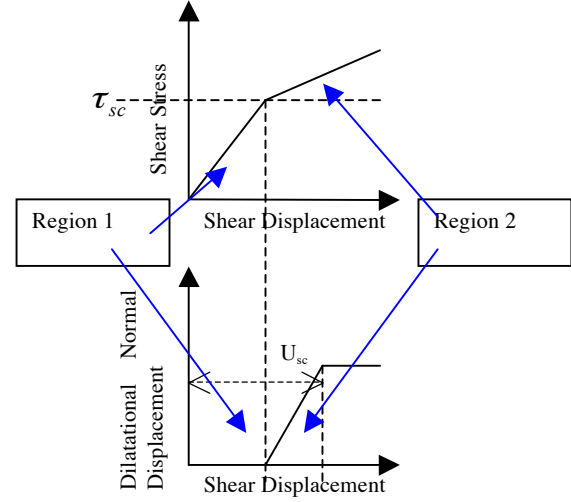


Figure 3. Strategy for modeling shear dilation

Calculation Procedure

When the stress ratio $K=0$, we can use the fracture-geometry information and mechanical information to calculate the initial total elastic compliance tensor and permeability tensor. When the stress ratio $K=1$, we first assign initial total elastic compliance tensor fields to each element in the FLAC3D model (employing a user-defined elastic anisotropic constitutive model) and calculate the new stress state. Note that because of the heterogeneous compliance within the model, with different compliance tensors for each element, the new stress state will be heterogeneous, somewhat different from the stress applied at boundaries. Then, we use the new stress fields to calculate the stress-induced fracture change and update the permeability tensor and compliance tensor fields. With the permeability tensor defined in each element, we use TOUGH2 to simulate the flow and transport through the model. The same procedures are used for stress ratios $K=2, 3$, and 5 . Consequently, the elastic stiffness and permeability tensors are updated anisotropically and heterogeneously, depending on the stress state when stress ratio K increases from 0 to 5 .

RESULTS AND DISCUSSION

We used a “multiple interacting continua” (MINC) method (Pruess and Narasimhan 1985) in TOUGH2 to perform the flow and transport simulation, which characterizes the rock-matrix-diffusion process in the solute transport simulation. One fracture continuum and three matrix continua were used in the MINC model. In the simulations presented in this paper, we divided the model domain into 40×40 elements of side length 0.5 m. TOUGH-FLAC results (denoted as LBNL) were compared with three other teams with different approaches. The IC team used a discrete fracture network (DFN) model with computer program NAPSAC, whereas KTH used the 2D discrete element code UDEC, and TUL used the combined DFN and EC (equivalent continuum) flow and solute transport simulation code FLOW123D. The approaches and results of other teams are described in Zhao et al (2012).

Figure 4 shows the resulting equivalent-modeling-domain permeability changes at different stress ratios. Permeability tensor fields under different stress ratios from $K=0$ to $K=5$ are shown in Figure 5. When the stress ratio K increases, the permeability of K_x and K_z within the modeling domain decreases correspondingly. We used the flow rate at a downstream outlet to inversely calculate the equivalent permeability. The results in Figure 4 are consistent with Figure 5 and are sensible. For example, assuming an increasing horizontal stress while keeping a constant vertical stress, it would be expected that the equivalent vertical permeability decreases much more than the equivalent horizontal permeability.

For the transport calculation, we used a solute transport approach, which can be described as follows: (1) zero initial concentration over the entire model; (2) a short interval of constant concentration at the inlet boundary; (3) thereafter, zero concentration inflow along all the boundaries, including the lateral sides parallel to the macroscopic flow direction.

Under the high hydraulic pressure gradient of 10^4 Pa/m, advection is the main “driving force” of solute transport. As shown in 6, under a high hydraulic gradient, a negligible amount of solute

diffuses into the rock matrix no matter what kind of stress state exists. The simulation results for the case of horizontal flow along a relatively high horizontal gradient are compared in terms of breakthrough curves in Figure 7. When $K=0$ (Figure 7a), the breakthrough curves given by the four teams are quite similar. When considering the stress effects (Figure 7b-d)), the four teams predicted a general shift in breakthrough curves in the longer time direction with increasing stress ratios.

The rock-matrix diffusion has an important influence on transport behavior under low hydraulic gradients (10 Pa/m) (Figure 8). The general trend of breakthrough curves shifting with increasing stress ratios was consistent with the high hydraulic gradient case. The much longer tails for breakthrough curves assuming matrix diffusion indicate that a portion of solute could stay in the matrix micropores for a long time before diffusing back to the fractures. Under a low hydraulic gradient, rock-matrix diffusion will retard solute transport. As shown in Figure 9, when the stress ratio increases, more solute will diffuse into the matrix, and as a result, solute transport will be strongly retarded.

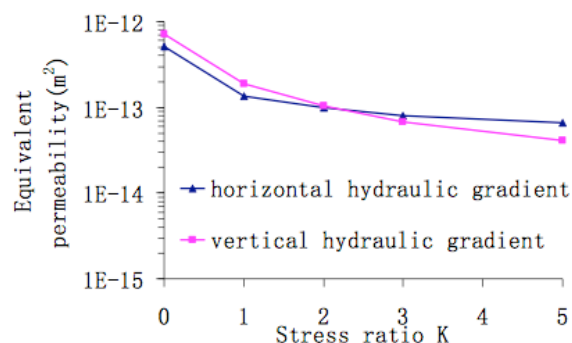


Figure 4. Equivalent permeability for horizontal and vertical flow at different stress ratios

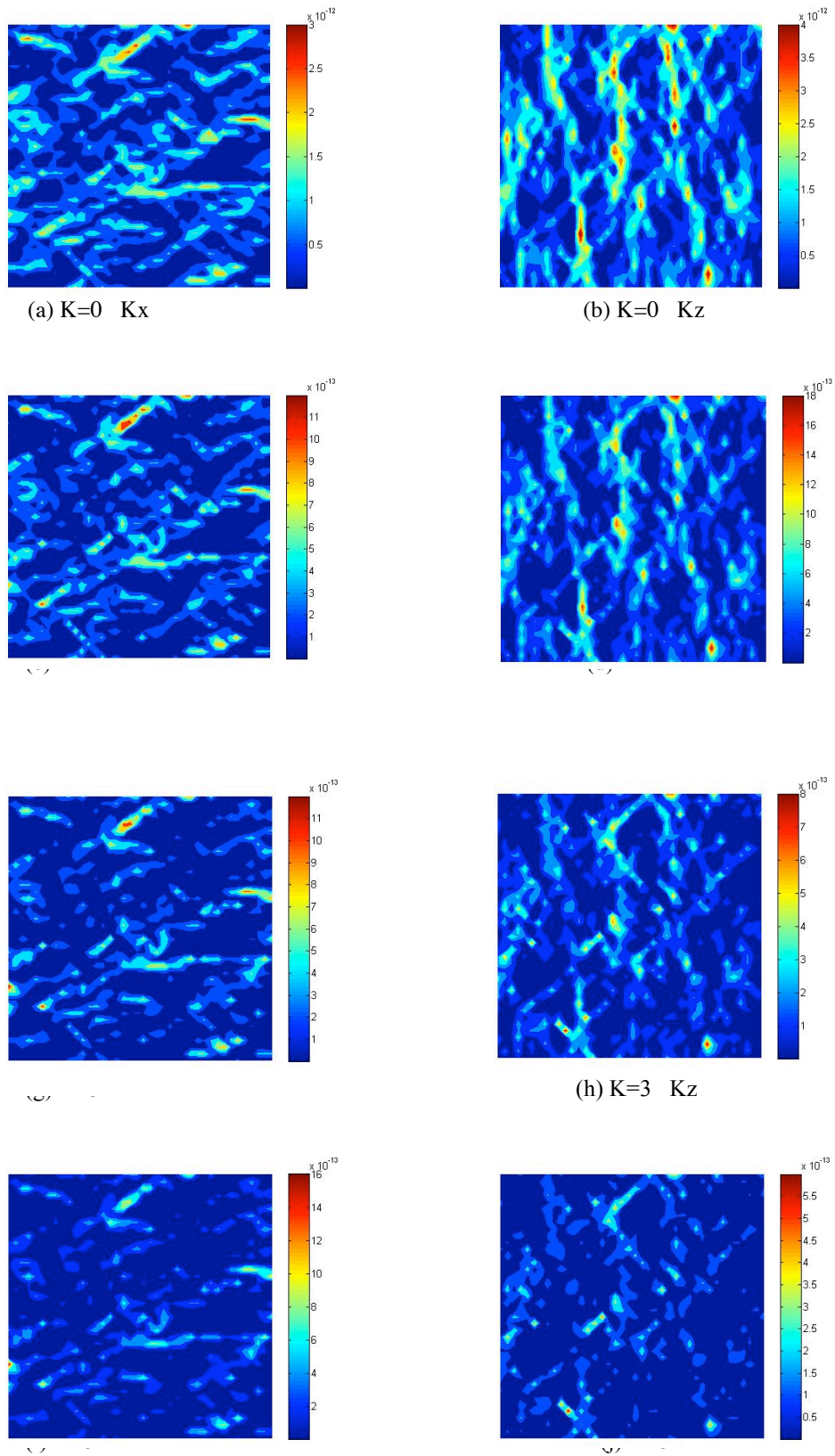
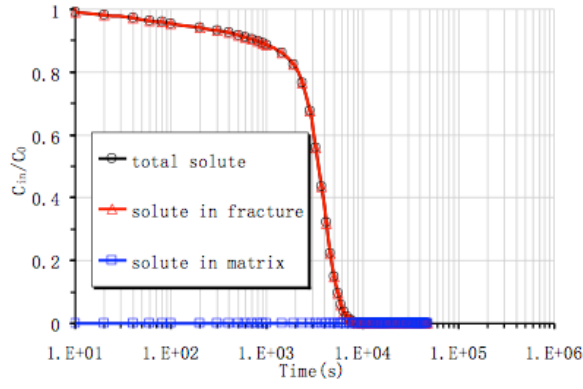
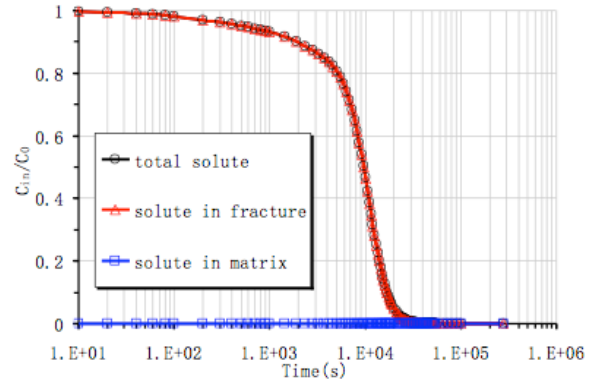


Figure 5. Permeability tensor fields with increasing stress ratio from $K=0$ to $K=5$

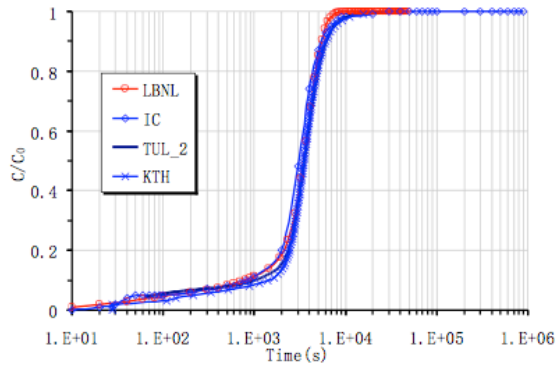


(a) K=0

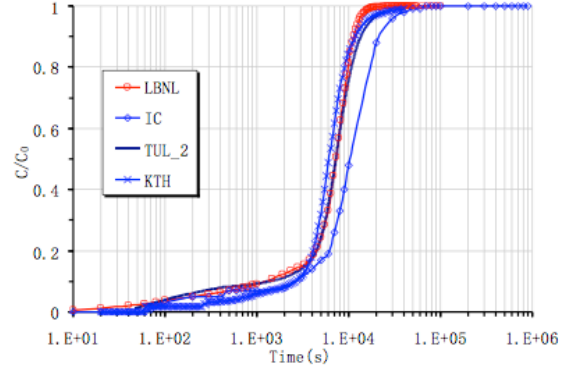


(b) K=5

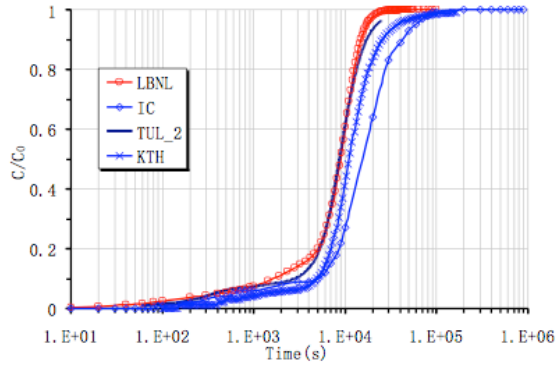
Figure 6. Solute concentration variation in fractures and rock matrix when K=0, 5 under a horizontal hydraulic gradient of 10^4 Pa



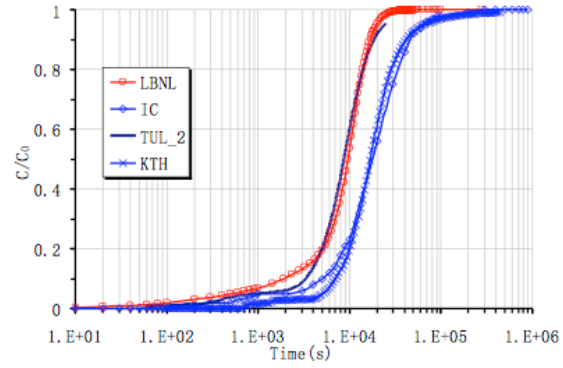
(a) K=0



(b) K=1



(c) K=3



(d) K=5

Figure 7. Comparison of breakthrough curves for conservative tracers exiting from all the three outlet boundaries with increasing stress ratio, under a horizontal hydraulic gradient of 10^4 Pa/m

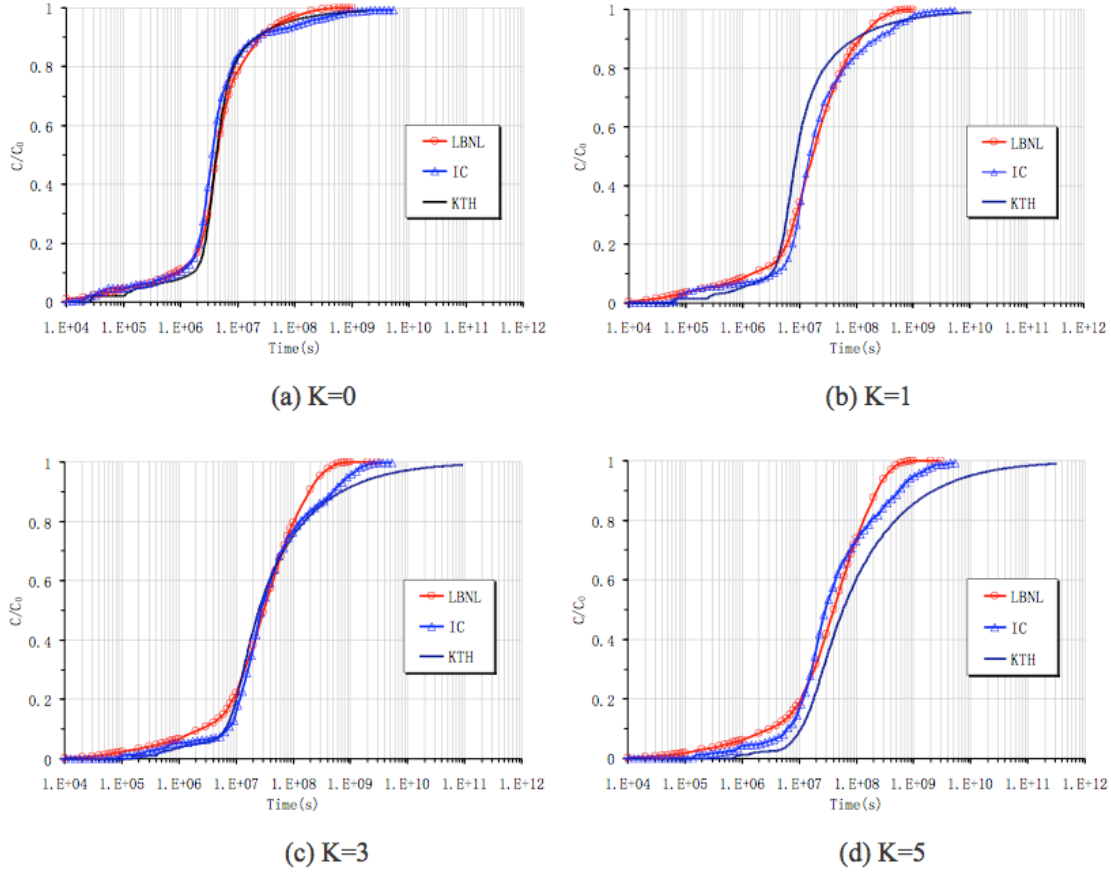


Figure 8. Comparison of breakthrough curves for interacting tracers exiting from all the three outlet boundaries with increasing stress ratio, under a horizontal hydraulic gradient of 10 Pa/m

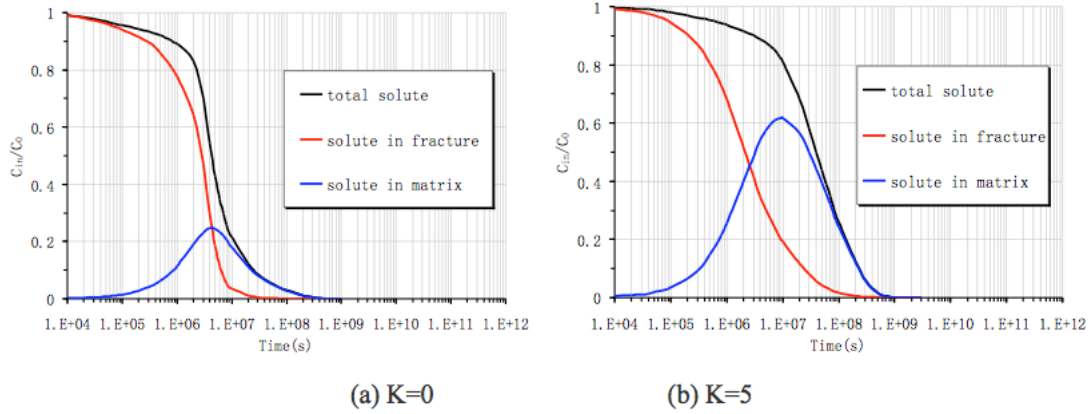


Figure 9. Solute concentration variation in fractures and rock matrix when $K=0, 5$ under a horizontal hydraulic gradient of 10 Pa/m

CONCLUDING REMARKS

In this paper, the stress effect on fluid flow and transport in fractured rock masses is investigated through a discrete continuum model derived from a modified crack tensor theory. We applied this methodology to a 2D benchmark test denoted as

Task C in the DECOVALEX-2011 project. Results were compared with other independent model simulation results, including discrete fracture models, and the result comparisons show good agreement. Some conclusions can also be drawn:

1. When the stress ratio increases, fractures aperture close, resulting in a reduction of permeability and porosity, and solute is significantly retarded as a result of the permeability reduction.
2. When the model is under a low hydraulic gradient, rock-matrix diffusion in addition to advection will play a very important part in solute transport, retarding the solute transport substantially.

In this paper, we applied a one-way coupled hydromechanical model, in which we considered the effects of stress-dependent permeability on the fluid flow, but not pore-pressure effects on fracture deformation. The one-way coupled approach is justifiable in this case, because the fluid pressure is very small compared to the applied stress. However, our approach can be readily extended and applied for two-way coupled problems, and this possibility will be the subject of future studies.

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